

# 3D Aircraft Control Surface Enabled by Co-Flow Jet Flap

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#### Abstract

This paper conducts Improved Delayed Detached Eddy Simulation to investigate the performance of a 3D aircraft control surface with Co-flow Jet (CFJ) active flow control applied on the flap with severe adverse pressure gradients (APG). For the numerical validation with the baseline control surfaces that have large flow separation, the predicted lift coefficient  $(C_L)$ , drag coefficient  $(C_D)$ , and pressure coefficient  $(C_n)$  distributions are in good agreement with the experiment at both deflection angle of 30° and 40°. The control surface using CFJ in the front main part with mild APG is also compared. With a small momentum coefficient  $(C_{\mu})$  of 0.025, the control surface using CFJ on the flap with severe APG outperforms the control surface using CFJ in the front main part in both control effectiveness and energy efficiency. Compared with the front CFJ control surface, the control surface with CFJ flap achieves 46.1% increase of lift coefficient with 80.8% lower power consumption. The improvement of the corrected aerodynamic efficiency  $\Delta(C_L/C_D)_c$  is increased by 30.8%. The CFJ flap control surface also outperforms the Front CFJ configuration at the high deflection angle ( $\delta$ ) of 50° with  $C_L$  increased by 44.8% and  $(C_L/C_D)_c$  increased by 6.8%. It can also attach the flow very well at  $\delta$  of 70° and achieves a lift coefficient more than twice larger than the baseline. Overall, the CFJ flap control surface is more effective than the Front CFJ control surface to overcome adverse pressure gradients with attached flow using a smaller  $C_{\mu}$ .

### Nomenclature

AoA	Angle of attack
AFC	Active Flow Control
C	Chord length
CFJ	Co-flow jet
$C_L$	Lift coefficient
$C_D$	Drag coefficient
$c_p$	Constant pressure specific heat
$C_p$	Pressure coefficient, $(P - P_{\infty})/(\frac{1}{2}\rho_{\infty}V_{\infty t}^2)$
$C_{\mu}$	Jet momentum coefficient, $\dot{m}_j V_j / (\frac{1}{2} \rho_{\infty} V_{\infty}^2 S)$
$C_L/C_D$	Aerodynamic efficiency
$(C_L/C_D)_c$	Aerodynamic efficiency corrected for CFJ airfoil

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D Total drag on the airfoil

FASIP Flow-Acoustics-Structure Interaction Package

 $H_t$  Total enthalpy

L Total lift on the airfoil

LE Leading Edge  $\dot{m}$  Mass flow rate

 $\overline{\dot{m}}$  Non-dimensional mass flow rate,  $\dot{m}/(V_{\infty}\rho_{\infty}S)$ 

Mach number

 $M_j$  Injection Mach number MAC mean aerodynamic chord P CFJ Pumping power

 $P_c$  Power coefficient,  $P/(\frac{1}{2}\rho_{\infty}V_{\infty}^3S)$ 

 $P_t$  Total pressure

 $P_{\infty}$  Static pressure of free-stream RANS Reynolds-Averaged Navier-Stokes

 $R_e$  Reynolds number

S Planform area of the wing

TE Trailing Edge  $T_t$  Total temperature  $V_{\infty}$  Free-stream velocity

 $V_{\infty t}$  Free-stream velocity normal to the wing LE, used to calculate  $C_p$ 

 $V_j$  Injection velocity ZNMF Zero-Net Mass Flux

c Subscript, stands for corrected

j Subscript, stands for jet

 $\alpha$  Angle of attack  $\beta$  Sideslip angle

γ Air specific heats ratio

 $\begin{array}{ccc} \Gamma & & \text{Total pressure ratio of CFJ pump} \\ \eta & & \text{CFJ pumping system efficiency} \end{array}$ 

 $\rho_{\infty}$  Free-stream density  $\delta$  Deflection angle

 $\theta_1$  Angle between the injection slot surface and a line normal to the airfoil chord Angle between the suction slot surface and a line normal to the airfoil chord

#### 1 Introduction

Aircraft control surfaces such as vertical tails, horizontal tails, and canards are responsible for maintaining aircraft stability. Control surfaces need to have high control authority by generating sufficient lift with rapid response time to keep the aircraft trimmed. To achieve such performance, control surfaces usually have large sizes, which bring severe penalties of weight, drag, and energy consumption.

Active Flow Control (AFC) as a mean to enhance lift has great potential to reduce the size and weight of control surfaces [1, 2, 3, 4, 5, 6, 7]. AFC is used to control the separated flow of vertical tails to enhance aerodynamic performance and mitigate flutter [8, 9, 10, 11, 12, 13, 14, 15, 16, 17]. The research

of Boeing and NASA [8, 9, 10, 11, 12, 13, 14, 15] on vertical tails using sweeping jets and synthetic jets AFC represents the state of the art. Rathay et.al [8] conducted wind tunnel experiments on a swept and tapered tail with a 29.6% chord rudder. Using flow control, the side force was increased by up to 18% at moderate rudder deflections with the AFC actuators operating at dimensionless frequency of O (10) [8] and a momentum coefficient  $C_{\mu}$ =0.00721. Compared with synthetic jets, sweeping jets have higher  $C_{\mu}$  output and corresponding jet velocity. Thus sweeping jets were selected over the synthetic jets by Boeing/NASA team for the subsequent full-scale AFC wind tunnel tests [9, 10].

The vertical tails with sweeping jets AFC were successfully tested on subscale models [11, 12], full-scale models [9, 10] and finally in flight [9]. The subscale test was performed at a 14% scaled model of Caltech and more than 50% of the side force enhancement was achieved by sweeping jet actuation with the momentum coefficient  $C_{\mu}$  of 0.017. The full-scale vertical tail model equipped with sweeping jets AFC was tested at a nominal speed of 100 knots ( $M_{\infty} \sim 0.15$ , Re  $\sim 15$  million), a maximum speed of 130 knots ( $M_{\infty} \sim 0.2$ , Re  $\sim 20$  million), and across the vertical tail flight envelop for rudder deflections (0° to 30°) and sideslip angles ( $0^{\circ}$  to  $-7.5^{\circ}$ ). A 31-actuator sweeping jets configuration produces significant flow attachment on the rudder, which results in 20% increase in side force for the maximum rudder deflection of 30° at the sideslip angle of 0° and -7.5°. Subsequently, the sweeping jets-enhanced vertical tail was flown on the Boeing 757 ecoDemonstrator in the spring of 2015. A side force increase of 13% to 16% was estimated at a  $30^{\circ}$  rudder deflection for the critical sideslip angle range between  $0^{\circ}$  and  $-7.5^{\circ}$  with the sweeping jets. Kara [16, 17] analyzed the complex flow inside the sweeping jets for design optimization of actuator geometry with minimum pressure loss. However, the sweeping jets tend to suffer large energy loss due to the jet sweeping, 360° turning and massive flow separation. Furthermore, the system will also suffer an energy penalty due to introducing the air flow from engine bleed. The other challenging issue using engine bleed for flow control is that when the engines are idle at landing, they may not be able to provide sufficient mass flow.

Recently, Xu and Zha [18, 19] apply co-flow jet (CFJ) active flow control on the main part (front part before flap) of the 3D vertical tail control surface, which achieves substantial lift enhancement at low energy expenditure. Co-flow Jet (CFJ) airfoil [2, 5, 20, 21, 22, 23, 24, 25, 26, 27, 28] is a zero-net mass flux (ZNMF) flow control that does not need to use engine bleed. The advantage of applying CFJ on the front main part of a control surface is that the inner space is larger to facilitate embedding the CFJ actuators than the space of the flap. This is particularly true for small general aviation and unmanned aircraft. However, severe adverse pressure gradient (APG) and flow separation occur on the flap when it is deflected. The front part of a control surface has mild APG because it is aligned with the freestream flow. Our recent studies on the NASA hump [29, 30] indicate that applying CFJ in APG is more efficient and effective than in mild APG or favorable pressure gradient (FPG). This motivates the present study to apply the CFJ on the flap in severe APG. Compared with CFJ applied in the front part, applying CFJ on the flap is much more effective to increase the lift coefficient and requires a lower energy expenditure.

#### 1.1 Co-Flow Jet

In the CFJ wing, an injection slot near leading edge (LE) and a suction slot near trailing edge (TE) on the wing suction surface are created as shown in Fig. 1. A small amount of mass flow is drawn into the wing near the TE, pressurized and energized by a micro-compressor pumping system inside the wing, and injected near the LE tangential to the main flow. The whole process does not add any mass flow to the system and hence is a ZNMF flow control.

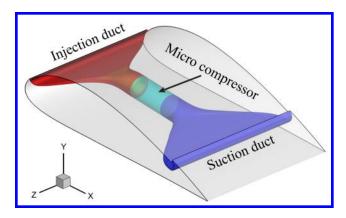


Figure 1: Schematics of the CFJ wing.

As described in [31, 32], a symmetric CFJ airfoil is used for the control surface as shown in Fig. 2. The injection slot and the suction slot are distributed on both sides of the CFJ control surface airfoil. When one side CFJ is working to generate side force, the other side CFJ is closed. The 3D CFJ control surface is created by extruding and tapering the 2D CFJ airfoil in a spanwise direction.

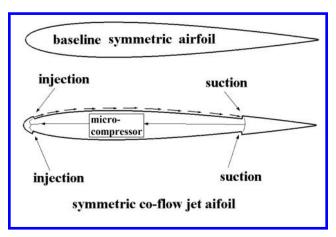


Figure 2: Schematics of the baseline and the CFJ control surface airfoils.

## 2 CFJ Parameters

This section lists the important parameters used to evaluate aerodynamic performance of a CFJ airfoil.

#### 2.1 Jet Momentum Coefficient

The jet momentum coefficient  $C_{\mu}$  is a parameter used to quantify the jet intensity. It is defined as:

$$C_{\mu} = \frac{\dot{m}V_j}{\frac{1}{2}\rho_{\infty}V_{\infty}^2 S} \tag{1}$$

where  $\dot{m}$  is the injection mass flow,  $V_j$  is the mass-averaged injection velocity,  $\rho_{\infty}$  and  $V_{\infty}$  denote the free stream density and velocity, and S is the planform area.

#### 2.2 Lift and Drag Calculation

For CFD simulation, the full reactionary forces produced by the momentum and pressure at the injection and suction slots are included by using control volume analysis. Zha et al.[20] gives the following formulations to calculate the lift and drag due to the jet reactionary force for a CFJ airfoil. By considering the effects of injection and suction jets on the CFJ airfoil, the expressions for these reactionary forces are given as:

$$F_{x_{cfj}} = (\dot{m}_j V_{j1} + p_{j1} A_{j1}) * \cos(\theta_1 - \alpha) - (\dot{m}_j V_{j2} + p_{j2} A_{j2}) * \cos(\theta_2 + \alpha)$$
(2)

$$F_{y_{cfj}} = (\dot{m}_{j1}V_{j1} + p_{j1}A_{j1}) * sin(\theta_1 - \alpha) + (\dot{m}_{j2}V_{j2} + p_{j2}A_{j2}) * sin(\theta_2 + \alpha)$$
(3)

where the subscripts 1 and 2 stand for the injection and suction respectively, and  $\theta_1$  and  $\theta_2$  are the angles between the injection and suction slot's surface and a line normal to the airfoil chord.  $\alpha$  is the angle of attack.

The total lift and drag on the airfoil can then be expressed as:

$$D = R_x' - F_{x_{cfj}} \tag{4}$$

$$L = R_y' - F_{y_{cfi}} \tag{5}$$

where  $R'_x$  and  $R'_y$  are the surface integral of pressure and shear stress in x (drag) and y (lift) direction excluding the internal ducts of injection and suction. For CFJ wing simulations, the total lift and drag are calculated by integrating Eqs.(4) and (5) in the spanwise direction.

#### 2.3 Power Coefficient

The power consumption is determined by the jet mass flow and total enthalpy change as the following:

$$P = \dot{m}(H_{t1} - H_{t2}) \tag{6}$$

where  $H_{t1}$  and  $H_{t2}$  are the mass-averaged total enthalpy in the injection cavity and suction cavity respectively, P is the power required by the pump and  $\dot{m}$  the jet mass flow rate. Introducing  $P_{t1}$  and  $P_{t2}$  as the mass-averaged total pressure in the injection and suction cavity respectively, the pump efficiency  $\eta$  and the total pressure ratio of the pump  $\Gamma = \frac{P_{t1}}{P_{t2}}$ , the power consumption is expressed as:

$$P = \frac{\dot{m}c_p T_{t2}}{\eta} \left(\Gamma^{\frac{\gamma - 1}{\gamma}} - 1\right) \tag{7}$$

where  $\gamma$  is the specific heat ratio equal to 1.4 for air,  $\eta$  is the micro-compressor efficiency with a typical value of 80% [28, 33], but in this paper, it is assumed as 100% to provide the required CFJ power. Eq. (7)

indicates that the power required for CFJ is linearly determined by the mass flow rate and exponentially by the total pressure ratio. This relationship in fact applies to all the active flow controls based on fluidic actuation. Thus,  $C_{\mu}$  is not a suitable parameter to represent the power consumption of active flow control [5, 34, 35]. For example, a high  $C_{\mu}$  could have a substantially lower power consumption than a lower  $C_{\mu}$  if the large  $C_{\mu}$  is created by a high mass flow rate and low jet velocity, which only needs a low total pressure ratio [5, 34, 35]. Since CFJ flow control is zero-net-mass-flux, all the mass flow is generated locally and a high mass flow or high  $C_{\mu}$  is not a limitation for CFJ application. This is very different from the circulation control (CC) airfoil, for which the mass flow needs to be introduced from an external source (e.g., engine bleed).

The power coefficient is expressed as:

$$P_c = \frac{P}{\frac{1}{2}\rho_{\infty}V_{\infty}^3 S} \tag{8}$$

## 2.4 Corrected Aerodynamic Efficiency

The conventional wing aerodynamic efficiency is defined as:

$$\frac{C_L}{C_D} \tag{9}$$

For the CFJ wing, the ratio above still represents the pure aerodynamic relationship between lift and drag. However, since CFJ active flow control consumes energy, the ratio above is modified to take into account the energy consumption of the pump. The formulation of the corrected aerodynamic efficiency for CFJ wings is:

$$\left(\frac{C_L}{C_D}\right)_c = \frac{C_L}{C_D + P_c} \tag{10}$$

where  $P_c$  is the power coefficient, L and D are the lift and drag generated by the CFJ wing. The formulation above converts the power consumed by the CFJ into a force  $\frac{P}{V_{\infty}}$  which is added to the aero-dynamic drag D. If the pumping power is set to 0, this formulation returns to the aero-dynamic efficiency of a conventional wing.

## 3 Numerical Algorithms

The in-house high order accuracy CFD code Flow-Acoustics-Structure Interaction Package (FASIP) is used to conduct the numerical simulation. The 3D Improved Delayed Detached Eddy Simulation (IDDES) [36, 37, 38, 39] turbulence model is used. A 3rd order WENO scheme for the inviscid flux [40, 41, 42] and a 2nd order central differencing for the viscous terms are employed to discretize the Navier-Stokes equations. The low diffusion Roe scheme used as the approximate Riemann solver is utilized with the WENO scheme to evaluate the inviscid fluxes. Implicit time marching method using Gauss-Seidel line relaxation is used to achieve a fast convergence rate [43]. Parallel computing is implemented to save wall clock simulation time [44]. The FASIP code is intensively validated for various steady and unsteady 2D and 3D flows

including full aircraft [25, 45, 46], multi-stage compressors [47, 48, 49, 50, 49, 51], aero-elasticity flows [52, 53, 54, 55, 56, 57] and for CFJ 2D and 3D airfoil simulations [5, 20, 21, 22, 25, 26, 27, 39, 58, 59, 60]. Since the experimental results reported are time-averaged steady state results, the numerical results are also presented as the time-averaged results after the flow and all the aerodynamic forces become statistically stable.

## 4 Baseline Control Surface Validation

The baseline control surface model used in the present paper is adopted from the previous study [18], which is originally tested and simulated in [9, 10, 11, 12, 61]. The baseline vertical tail is tapered, swept with 42° and stacked using NACA0012 airfoil. The aspect ratio based on mean aerodynamic chord (MAC) is 1.98. Details of geometry are described in Ref. [18]. The free-stream conditions used in the present study are the same conditions as given by Seele et al in the experiment [12], which has the Reynolds number,  $Re_{\infty}=1.36\times10^6$ , incoming flow velocity,  $V_{\infty}=40$  m/s (about Mach 0.12), and sideslip angle  $\beta=0^{\circ}$ . The front part of the control surface root is installed on the bottom wall. There is a small clearance between the flap and the wall resulting from flap deflection, and is simulated in this study as well as in the previous ones [18].

The computational domain is meshed using an O-type grid with a mesh size of 6.14 million cells (480  $\times$  80  $\times$  160). The results are stable after the characteristic time of 20 where the standard deviation (SD) of  $C_L$  and  $C_D$  for the last 200 time-step is in the order of  $10^{-9}$  to  $10^{-5}$ , and are virtually the machine zero compared with the  $C_L$  and  $C_D$  at order of 1. Details of mesh topology, boundary condition set-up and convergence history are presented in Ref. [18]. With the present mesh size, the predicted results achieve a good agreement with the experimental data with the  $C_L$  deviation of 3.8% and  $C_D$  deviation of 3.6% considering the massively separated flow due to the 30° deflected flap.

The computed results are further validated by examining the wing surface pressure coefficient distributions  $(C_p)$  at two deflection angles ( $\delta = 30^{\circ}$  and  $40^{\circ}$ ). At each  $\delta$ , two of three spanwise locations shown in Fig. 3 are selected for comparison, middle (70% span of at LE) and outboard (89% span of at LE). The inboard (40% span of LE) comparison is presented in Ref. [18]. As shown in Fig. 4, the pressure coefficient predicted by the present IDDES agrees well with the experimental data at  $\delta = 30^{\circ}$  and is slightly under estimated at  $\delta = 40^{\circ}$ , whereas the simulation of Vatsa et al [61] over-predicts the pressure on the pressure surface for both two span locations at two  $\delta$  angles. Mesh refinement study is conducted by doubling the number of cells in i, j, k direction respectively as  $960 \times 80 \times 160$ ,  $480 \times 160 \times 160$  and  $480 \times 80 \times 320$ . It is demonstrated in Ref. [18] that the numerical results of the baseline control surface are converged based on the initial mesh size of 6.14 million.

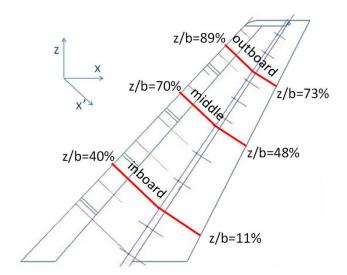


Figure 3: Illustration of span-wise pressure tap rows (picture adopted from [61]).

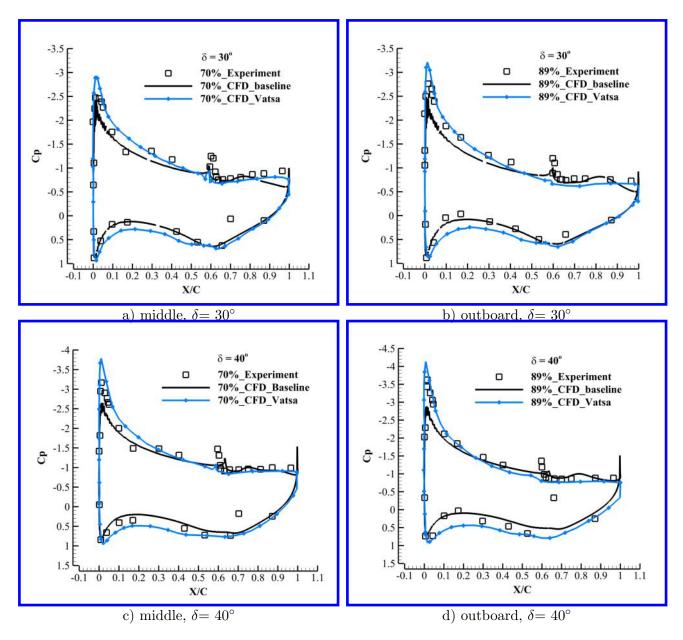


Figure 4:  $C_p$  comparisons of the baseline control surface at two deflection angles and two spanwise locations.

#### 5 3D CFJ Control Surface

A 3D CFJ control surface is created based on the baseline configuration by adding an injection slot and suction slot. The previous study [18] has the CFJ applied on the front main part of the control surface as shown in Fig. 5 (a), which has the injection slot located at 4%C from the leading edge and the suction (blue) slot located at 63%C upstream of the flap. The mixing between CFJ and mainflow occurs in a mild adverse pressure gradient, which is named as Front CFJ. This paper studies a new configuration as shown in Fig. 5 (right) that the CFJ is applied on the flap with the injection located at 66%C from the leading edge and the suction is moved further downstream to 85%C. The new configuration is named Flap CFJ.

The injection slot size for the Flap CFJ control surface is 0.45%C and the suction slot size is 1%C.

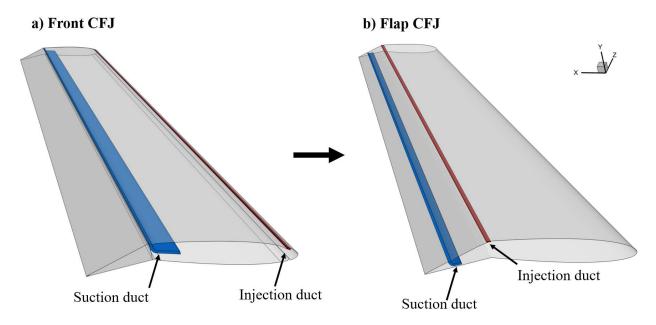


Figure 5: Geometry of the 3D CFJ control surfaces.

The mesh refinement study is also conducted for the control surface of Flap CFJ. The case showing the mesh refinement study herein has  $C_{\mu}$ =0.025,  $\beta$ =0°, and  $\delta$ =30°. The number of cells in i, j, k directions of CFJ are doubled respectively for the mesh refinement study. As presented in Table 1, the maximum variation of  $C_L$ ,  $C_D$  and  $(C_L/C_D)_c$  (defined in Eq. (10)) are 0.55%, 1.83% and 2.2%. Fig. 6 compares the  $C_p$  distributions calculated by the baseline mesh and refined mesh at two spanwise locations, which are virtually overlapped. These mesh refinement results demonstrate that the CFD solution is mesh independent.

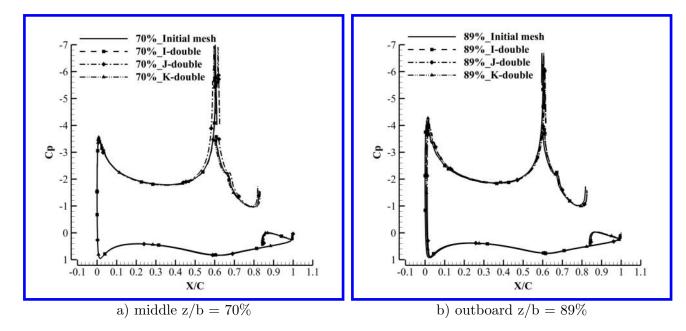


Figure 6:  $C_p$  distribution comparisons of the mesh refinement study of the Flap CFJ control surface at mid- and outer-span with  $C_{\mu}$ =0.025,  $\beta$ =0°, and  $\delta$ =30°.

Table 1: Mesh refinement studies of the Flap CFJ control surface with  $C_u$ =0.025,  $\beta$ =0°, and  $\delta$ =30°

Cases	Mesh size of CFJ	$C_L$	$\Delta C_L$	$C_D$	$\Delta C_D$	$(C_L/C_D)_c$	$\Delta (C_L/C_D)_c$
Baseline mesh	$125\times40\times60$	1.096	-	0.114	-	9.243	-
Doubled in i-direction	$250\times40\times60$	1.093	0.28%	0.114	0.40%	9.034	2.20%
Doubled in j-direction	$125\times80\times60$	1.093	0.26%	0.113	1.83%	9.382	1.50%
Doubled in k-direction	$125\times40\times120$	1.101	0.55%	0.115	1.30%	9.227	0.17%

## 5.1 Jet Momentum Coefficient $(C_{\mu})$ Trade Study

The trade study with the jet momentum coefficients  $C_{\mu}$  of 0.025, 0.05, 0.1, 0.2, and 0.26 is conducted to compare the aerodynamic performance for the Front CFJ and Flap CFJ control surfaces. The baseline control surface without CFJ is also presented as a reference. The sideslip angle ( $\beta$ ) is fixed at 0° and the flap deflection angle ( $\delta$ ) is fixed at 30°. Table. 2 compares the aerodynamic performance of the baseline, Front CFJ at  $C_{\mu}$ =0.025 and Flap CFJ cases at various  $C_{\mu}$ . Compared with the baseline control surface, both the Front and Flap CFJ cases largely increase the lift coefficient  $C_L$  by 28.1% and 46.1% respectively at  $C_{\mu}$  of 0.025. Clearly, the Flap CFJ is much more effective to increase the lift coefficient. Furthermore, the power coefficient of the Flap CFJ is 81% smaller than the Front CFJ case. This results in an increase of  $(C_L/C_D)_C$  by 32.8% and 30.3% respectively compared with that of the baseline and Front CFJ configuration. In other words, the CFJ control surface with CFJ applied at the front or flap is able to achieve a significant control effectiveness while maintaining a high energy efficiency.

Table 2: Aerodynamic performance of the control surface with different  $C_{\mu}$ 

Cases	$C_{\mu}$	$C_L$	$\Delta C_L$	$C_D$	$P_c$	$C_L/C_D$	$(C_L/C_D)_c$	$\Delta (C_L/C_D)_c$	Γ
Baseline EXP [61]		0.78	-	0.112	-	6.96	6.96	-	-
Baseline CFD	-	0.75	-	0.108	-	6.93	6.93	-	-
Front CFJ	0.025	0.96	28.1%	0.109	0.026	8.84	7.09	2.3%	1.02
Flap CFJ	0.025	1.095	46.1%	0.113	0.005	9.65	9.24	33.1%	1.006
Flap CFJ	0.05	1.166	55.5%	0.115	0.017	10.16	8.85	27.5%	1.013
Flap CFJ	0.1	1.234	64.5%	0.104	0.054	11.89	7.79	12.1%	1.030
Flap CFJ	0.2	1.323	76.4%	0.076	0.217	17.35	4.51	-35.0%	1.083
Flap CFJ	0.26	1.365	82.0%	0.056	0.461	24.36	2.64	-62.0%	1.154

Fig. 7 compares the aerodynamic performance between the Front and Flap CFJ at various  $C_{\mu}$  with the data of Front CFJ adopted from our previous work [18]. Baseline case is shown in the blue line as a reference. As shown in Fig. 7 (a), at the small  $C_{\mu}$  regime below 0.05, the lift coefficient of the Flap CFJ control surface is higher than the FPG injection, whereas the Front CFJ performs better at the high  $C_{\mu}$  regime. This is because applying CFJ at flap, the adverse pressure gradient (APG) region is more efficient and effective to remove flow separation [29, 30]. In other words, APG injection achieves a better attachment with a smaller  $C_{\mu}$ . In fact, at the small  $C_{\mu}$  of 0.025 and 0.05, the Flap CFJ achieves a higher improvement of lift ( $\Delta C_L$ ) and corrected aerodynamic efficiency  $\Delta (C_L/C_D)_c$  simultaneously, as compared to the Front CFJ. Fig. 7 (b) shows that both CFJ configurations have  $C_D$  reduced with the increasing of  $C_{\mu}$ . The power coefficient increases significantly with the  $C_{\mu}$  increase as shown in Fig. 7 (d). This is because  $P_c$  is exponentially determined by the total pressure ratio ( $\Gamma$ , Fig. 7 (f)) of CFJ micro-compressor actuator. A high  $\Gamma$  therefore leads to a much higher  $P_c$ . The flap CFJ has a lower  $P_c$  in all  $C_{\mu}$  and as a result, its  $(C_L/C_D)_c$  is boosted as illustrated in Fig. 7 (e).

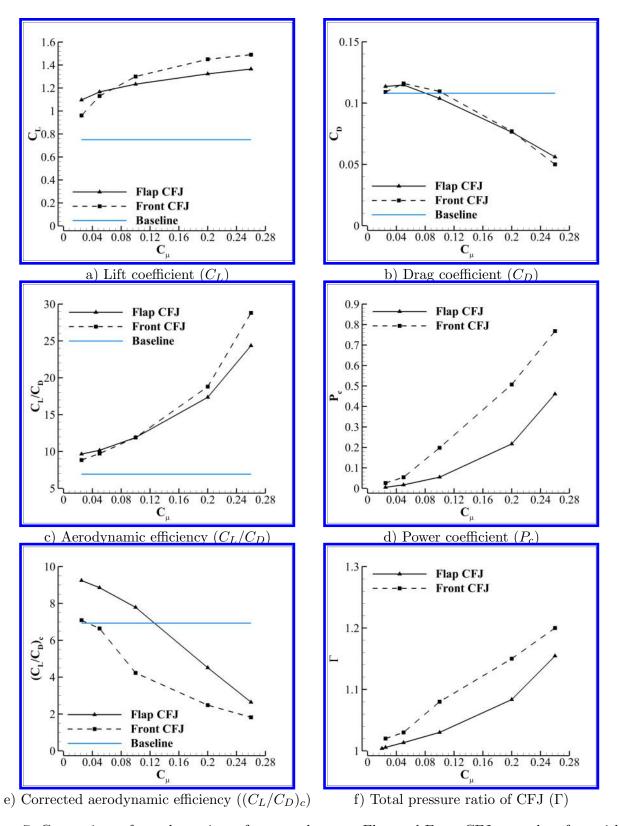


Figure 7: Comparison of aerodynamic performance between Flap and Front CFJ control surface with various  $C_{\mu}$ ,  $\beta=0^{\circ}$ , and  $\delta=30^{\circ}$ .

Since the Flap CFJ achieves both high effectiveness and efficiency at  $C_{\mu}$ =0.025, its flow-field compared with the Baseline and Front CFJ illustrated by Mach-number-colored streamlines is shown in Fig. 8. Severe flow separation is observed at the flap region of the baseline control surface as shown in Fig. 8 (a). With CFJ applied in the front region in Fig. 8 (b), flow separation at the flap region is largely suppressed but spanwise flow migration can be still clearly seen. The Flap CFJ has streamlines well aligned in the streamwise direction with much less spanwise flow migration, which also mitigates the tip vortex. This is because applying CFJ near separation onset location where the flap starts to deflect is the most effective to suppress flow separation [29, 30]. Such high control effectiveness is also evidenced by  $C_p$  distributions in Fig. 9. At both middle and outboard span-locations, the Flap CFJ achieves a much lower pressure on the suction surface at the flap region (X/C = 0.63 - 1.0).

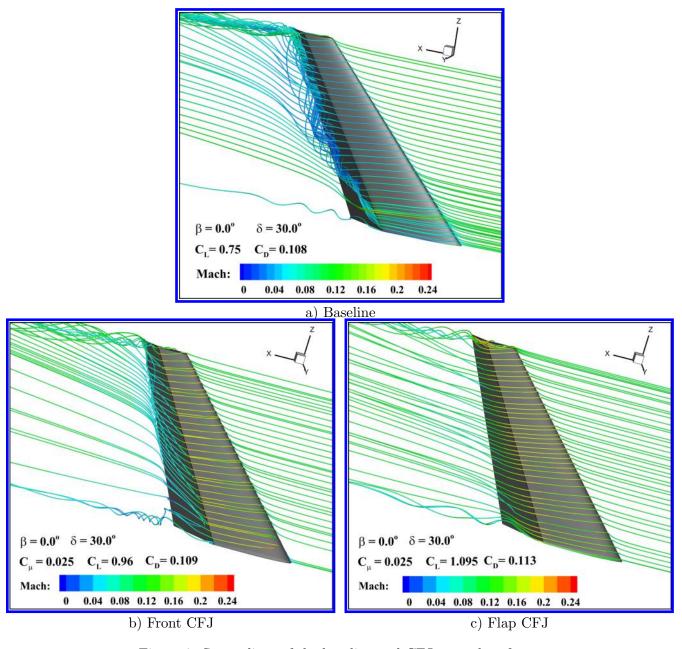


Figure 8: Streamlines of the baseline and CFJ control surfaces

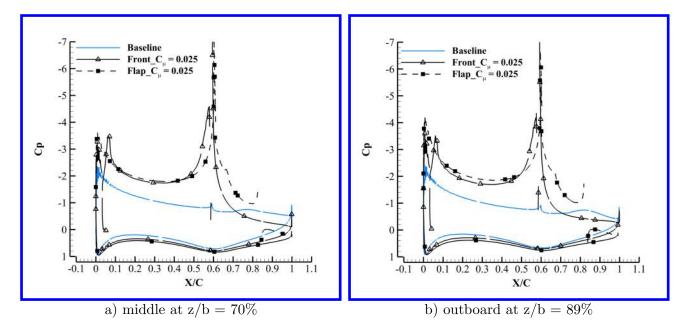


Figure 9:  $C_p$  distribution comparisons of Front and Flap CFJ control surface at mid- and outer-span with  $C_{\mu}$ =0.025,  $\beta$ =0°, and  $\delta$ =30°.

#### 5.2 Deflection angle ( $\delta$ ) Variation

This section studies the effects of the deflection angle  $(\delta)$  variation on the performance of the Flap CFJ control surface. Results are presented with two  $C_{\mu}$  of 0.05 and 0.2 representing the low and high jet intensity respectively. Four deflection angles of 30°, 40°, 50°, and 70° are studied for the Flap CFJ control surface, the Front CFJ configuration only has the results presented for the deflection angle of 30, 40 and 50, which were simulated in the previous study [18] and are used here for comparison.

Fig. 10 plots the  $C_L$ ,  $C_D$ ,  $P_c$ , and  $(C_L/C_D)_c$  varying with  $\delta$  angles for the Flap CFJ (solid line) and Front CFJ (dashed line) with  $C_{\mu}$  of 0.05 (hollow symbols) and 0.2 (solid symbols). The performance of the baseline control surface is plotted by the blue lines where its  $(C_L/C_D)_c$  is plotted in Fig. 10 (d) instead of  $(C_L/C_D)$ . With a small  $C_\mu$ =0.05, Flap CFJ achieves a higher  $C_L$  than the Front CFJ in all  $\delta$  angles due to the effective control of the flow separation at the flap region. The control effectiveness of the Front CFJ at the small  $C_{\mu}$  is weakening towards the high  $\delta$  because the flow separation is too severe to control at the high defection angle. Comparatively, solid lift enhancements are still achieved in the Flap CFJ, even at  $\delta=70^{\circ}$ . With a high  $C_{\mu}$  of 0.2 applied, the Front CFJ has a higher  $C_{L}$  at the low  $\delta$  of 30° and 40° but is outperformed at a higher  $\delta$  angle, which is again due to the strong flow separation at the flap. For the drag coefficient shown in Fig. 10 (b), both configurations behave similarly that have an increasing drag with the increase of  $\delta$  angle. On the one hand, this is because pressure drag increases as the flap deflects more. On the other hand, as the flow separation is removed with a better attachment on the flap, flow accelerates at the deflection due to the high turning, which reduces the pressure on the suction side and contributes to drag increase. It is also noteworthy that the low  $C_{\mu}$  help reduce drag at a low deflection angle of 30° as compared to the baseline case. This is because the pressure increased by the removal of flow separation outweighs the pressure reduction from the jet attachment on the deflection region. Such drag reduction can be only achieved in low deflection angle cases. The power coefficient  $(P_c)$  varying with different  $\delta$  is shown in Fig. 10 (c). The Flap CFJ has a much lower  $P_c$  at low  $\delta$  angle conditions, about

1/3 of the Front CFJ with  $C_{\mu}$ =0.05 and  $\delta$ =30°. Such low  $P_c$  contributes to the high  $(C_L/C_D)_c$  as shown in Fig. 10 (d). Overall, the Flap CFJ is more effective to overcome adverse pressure gradients, which can remove flow separation with smaller  $C_{\mu}$  than the Front CFJ. Therefore, the control using Flap CFJ has both high effectiveness and efficiency. However, once flow attachment is achieved, further increasing  $C_{\mu}$  brings minor improvements compared to the Front CFJ.

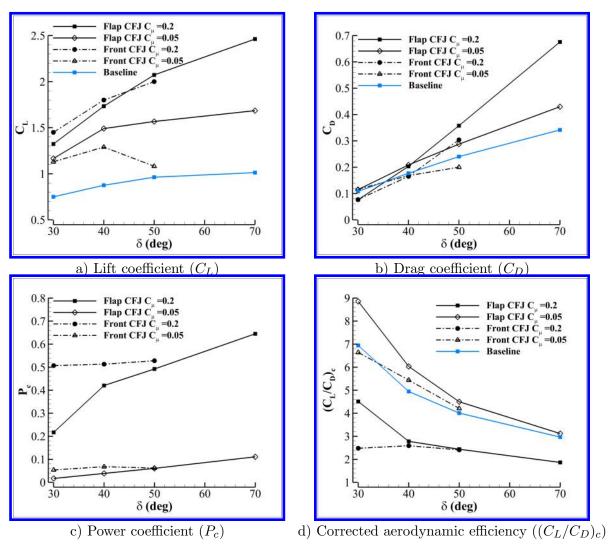


Figure 10: Comparison of aerodynamic performance between Flap and Front CFJ control surface with various  $\delta$ , and  $C_{\mu}$  of 0.05 and 0.2.

Fig. 11 shows the streamlines (colored by Mach number) of the Flap CFJ control surfaces at four deflection angles with  $C_{\mu}$ =0.2. The flow in all cases is well attached along the major span except the near tip and root regions. Flow accelerates at the locations that the flap deflects and the acceleration is enhanced with the increasing  $\delta$  angle due to the attached flows with a higher turning. The observed root vortex is caused by the gap between the deflected flap and the wall, which is intensified as the gap increases towards the high deflection angles. The tip vortex becomes very strong at  $\delta$  angle of 70° due to the enhanced pressure difference between the pressure and suction sides of the flap. However, the flow is still very well attached and aligned with the streamwise direction in the majority of the span. The lift

coefficient  $(C_L)$  at this condition is 2.46, a 125% increase compared with the baseline control surface. In principle, a CFJ control surface with 44% of the baseline control surface  $(C_L=1.09)$  can achieve the same side force, which would bring a substantial weight and drag reduction to the whole aircraft system.

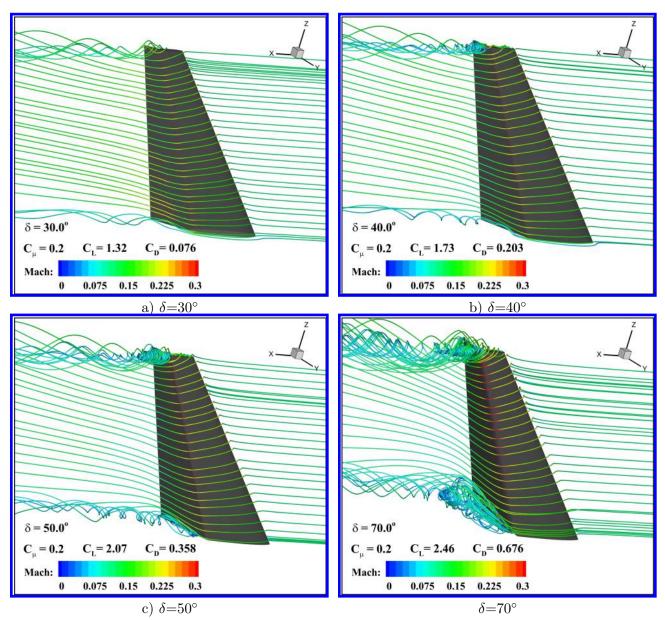


Figure 11: Streamlines of Flap CFJ cases with various  $\delta$  and  $C_{\mu}$  of 0.2.

## 6 Conclusion

Improved Delayed Detached Eddy Simulation is conducted to investigate the performance of a 3D aircraft control surface with Co-flow Jet (CFJ) active flow control applied on the flap with severe adverse pressure gradients (APG). The control surface using CFJ in the front main part with mild APG is also presented for comparison. With a small momentum coefficient ( $C_{\mu}$ ) of 0.025, the control surface using CFJ on the

flap with severe APG outperforms the control surface using CFJ in the front main part in both control effectiveness and energy efficiency. The control surface with CFJ flap achieves 46.1% increase of lift coefficient with 80.8% lower power consumption than the Front CFJ configuration. The improvement of the corrected aerodynamic efficiency  $\Delta(C_L/C_D)_c$  is increased by 30.8%. The CFJ flap control surface also outperforms the Front CFJ at the high deflection angle ( $\delta$ ) of 50° with  $C_L$  increased by 44.8% and  $(C_L/C_D)_c$  increased by 6.8%. It can also attach the flow very well at  $\delta$  of 70° and achieves a lift coefficient more than twice larger than the baseline. Overall, the CFJ flap control surface is more effective than the Front CFJ control surface to overcome adverse pressure gradients with attached flow using a smaller  $C_\mu$ .

## 7 Acknowledgment

The authors would like to acknowledge the computing resource provided by the Center for Computational Sciences at the University of Miami.

Disclosure: The University of Miami and Dr. Gecheng Zha may receive royalties for future commercialization of the intellectual property used in this study.

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